

# **Levelized Costs and Cost Risks of Electricity Generating Asset Portfolios**

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## Outline:

**Objective: Develop a method for approximating the probability distribution of the levelized cost of electricity ( *LC* ) for each generating technology and portfolios of generating technologies (providing a generalization of D'haeseleer, 2012)**

- (1) Define levelized cost, its mean, and variance => Monte Carlo simulation**
- (2) Identify cost drivers, parameters, and variables**
- (3) Approximate the probability densities of influential variables with historic data**
- (4) Simulate probability distributions of LC for nuclear power, CCGT, and coal**
- (5) Simulate probability distributions for combinations of generating technologies**
- (6) Discuss implications for electricity policy**
- (7) Identify topics for further research**

## Long-Run Average Levelized Cost:

See OECD-NEA-IEA, *Projected Costs of Generating Electricity* (2010, 2015)

$$LC = [CAPITAL(OC, r, It) + FUEL + O\&M] / E$$

**CAPITAL** is the product of Fixed Charge Rate and Total Capital Construction Costs, which depends on the Overnight costs, **OC**, cost of capital, **r**, and the lead time, **It**

**FUEL** is the *annual* fuel payment and a function of the amount of fuel and price of fuel

**O&M** is the *annual* Operations and Maintenance expense and Capital Additions, **CAPEX**

**E** is *annual* energy output equal to **MW · TT · CF**, i.e., the size of the generator in megawatts, **MW**, the total number of hours in a year, **TT**, and the Capacity Factor, **CF**

## What is the probability distribution of *LC* ?

# Mean and Variance of Levelized Cost:

$$LC = [CAPITAL(OC, r, It) + FUEL + O\&M] / E$$

$$E\{LC\} = E\{[CAPITAL(OC, r, It) + FUEL + O\&M] / E\}$$

$$VAR\{LC\} = E\{LC - E(LC)\}^2$$

- (1) Unfortunately, each element is likely to be a function of the size of the generator, MW
- (2) Therefore, the expectation of LC cannot be a simple ratio of the expectation of cost and the expectation of output (the numerator and denominator are correlated)
- (3) Further, calculating the variance is likely to be cumbersome given the underlying distributions

So, another strategy is used:

- (1) simulate the probability density of each important variable (calculate elasticity),
- (2) approximate the mean and variance with the moments of the probability distribution of the simulated value, and
- (3) conduct sensitivity analysis for important parameters

## Cost Drivers: Variables, Parameters, and Constraints

### Variables:

- OC** Construction Overnight Construction Cost
- It*** Construction Lead Time
- FUEL** is a function of quantities and prices of inputs (e.g., natural uranium, natural gas, coal)
- O&M** is a function of quantities and prices of labor and materials, etc.
- CF** Capacity Factor, is defined as  $E / MW \cdot TT$  (actual output/potential maximum output)

### Parameters:

- r*** is the Cost of Capital (assumed to be equal to real 5%, 7.5%, or 10%, as a function of the market)
- MW** is the size of the generator in megawatts, assumed to be fixed as a function of technology
- TT** is the total number of hours in a year, equal to 8,766 hours in an average year

### Constraints:

- (1) Simulated outcomes cannot be negative (hence, no symmetric input probability densities)
- (2) Input probability densities should have closed-form distributions (for transparency)
- (3) Output probability densities, when necessary for exposition, will be fitted to extreme value, exponential, normal, or lognormal (for comparability)

## Probability Density Functions in this Analysis:

**Extreme Value density:**  $\text{maxv}(\mathbf{a}, \mathbf{b}) = (1/\mathbf{b}) \cdot \mathbf{ab} \cdot \exp\{-\mathbf{ab}\}$ ,

**Extreme Value distribution:**  $\text{MAXV}(\mathbf{a}, \mathbf{b}) = \exp\{-\mathbf{ab}\}$ ,

where  $\mathbf{ab} = \exp\{-[(x - \mathbf{a})/\mathbf{b}]\}$  and

**a is the mode and the standard deviation is b times  $(\pi/\sqrt{6})$  ( $\approx 1.28$ ). The direction of the skewness in the extreme value distribution can be reversed, such that it has an extreme minimum value; this is designated here as  $\text{minv}(\mathbf{a}, \mathbf{b})$  and  $\text{MINV}(\mathbf{a}, \mathbf{b})$**

**Exponential density:**  $\text{expo}(\mathbf{b}) = [\exp(-x/\mathbf{b})]/\mathbf{b}$

**Exponential distribution:**  $\text{EXPO}(\mathbf{b}) = 1 - \exp(-x/\mathbf{b})$ ,

**where b and x must be greater than 0 (thus avoiding negative outcomes in simulation), and b is equal to the mean and the standard deviation (can include a shift parameter)**

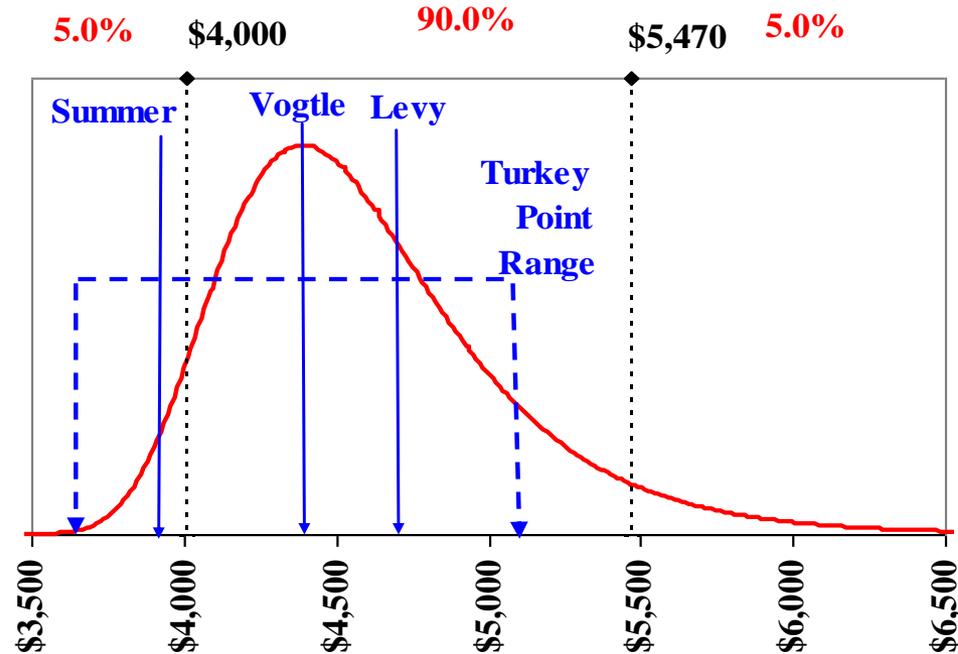
**Normal density**  $\text{normal}(\mu, \sigma^2) = (2\pi\sigma^2)^{-1/2} \cdot \exp\{-(x - \mu)^2 / (2 \cdot \sigma^2)\}$  and

**Lognormal density**  $\text{lognormal}(\mu, \sigma^2) = x^{-1} (2\pi\sigma^2)^{-1/2} \cdot \exp\{-(\ln x - \mu)^2 / (2 \cdot \sigma^2)\}$ ,

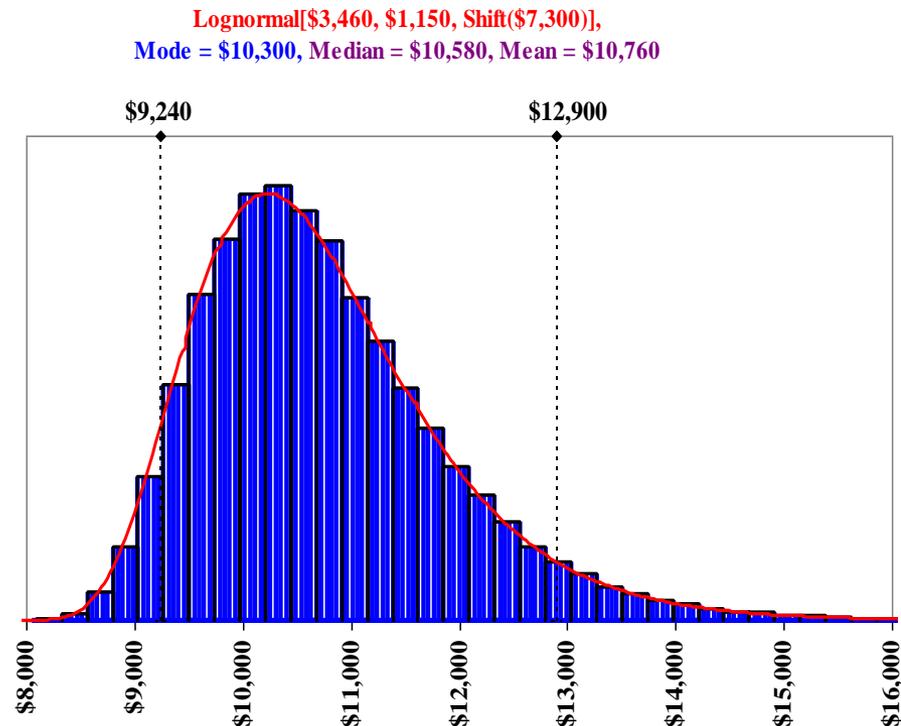
**where the  $\mu$  are the means and the  $\sigma^2$  are the variances**

## Overnight Construction Costs (AP1000) fitted to a extreme value density (2013\$):

Extreme Value,  $\max_v(\$4,400, \$360)$ ,  
 Mode = \$4,400, Mean = \$4,610, Median = \$4,530, SDev = \$460



**Total Construction Investment Costs (twin AP1000s)  
fitted to a lognormal density (2013\$,  $r = 7.5\%$ ):**  
**(compare to announcement of Kozloduy's AP1000 at \$5.3B,**  
<http://online.wsj.com/articles/bulgaria-signs-deal-with-westinghouse-on-nuclear-plant-1406890323>)



## ALWR Fuel Costs:

$$F_{MWh} = [ FC / (24 \cdot B \cdot \varepsilon) ] / CF, \text{ where}$$

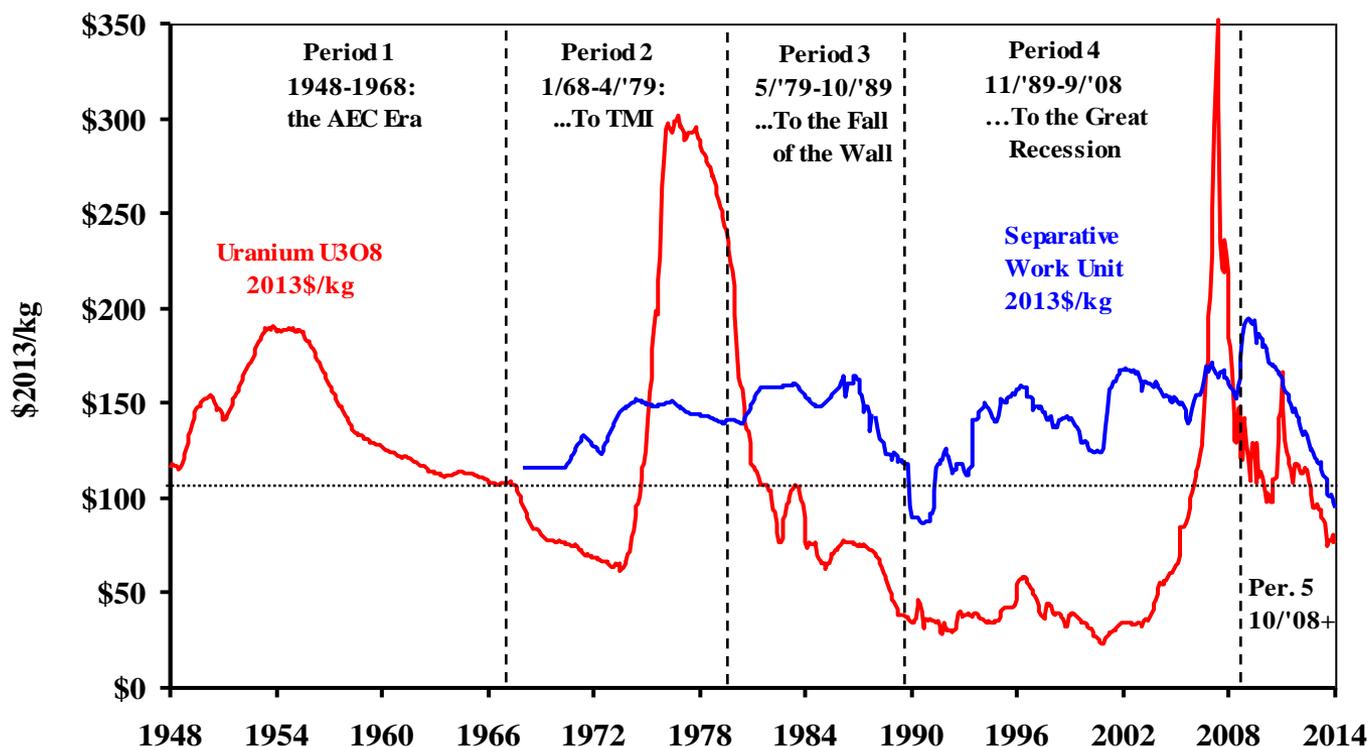
- (1) **FC** is the cost of nuclear fuel in dollars per kg
- (2) **24** is the number of thermal MWh in a thermal megawatt-day
- (3) **B** is the burnup rate measured in thermal megawatt-days per kgU
- (4) **ε** is the thermal efficiency of converting MW-thermal into MW-electric
- (5) **CF** is the capacity factor, assumed to be constant for all periods.

$$FC = RU \cdot P_{UF6} \cdot (1 + r)^{lt_U} + SWU \cdot P_{SWU} \cdot (1 + r)^{lt_S} + P_{FAB} \cdot (1 + r)^{lt_F}, \text{ where}$$

- (1) **RU** is the ratio of natural uranium input to enriched uranium output
- (2) **P<sub>UF6</sub>** is the price of natural uranium input plus its conversion to UF6
- (3) **SWU** is the number of Separative Work Units required in enrichment
- (4) **P<sub>SWU</sub>** is the price of enriching uranium hexafluoride, UF6
- (5) **P<sub>FAB</sub>** is the price of fabricating UO2 fuel from enriched UF6
- (6) **lt<sub>U</sub>**, **lt<sub>F</sub>**, and **lt<sub>S</sub>** are carrying times, e.g., 2.0, 1.0, 0.5 years, respectively

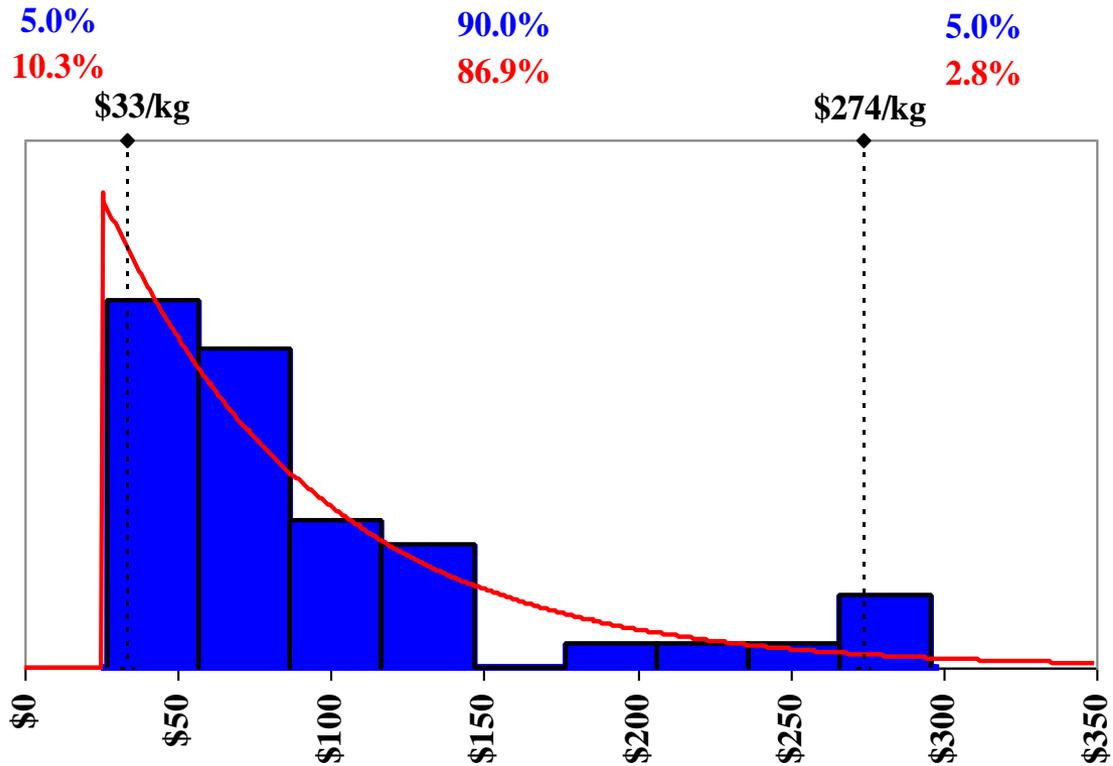
## Fuel Costs Depend on Costs of Uranium and Uranium Enrichment:

Sources: Prices 1948-1972 from US DOE (1981), 1973-2006 from ABARES (2007), and 2006-2014 from UXC website <http://www.uxc.com/review/UxCPrices.aspx>



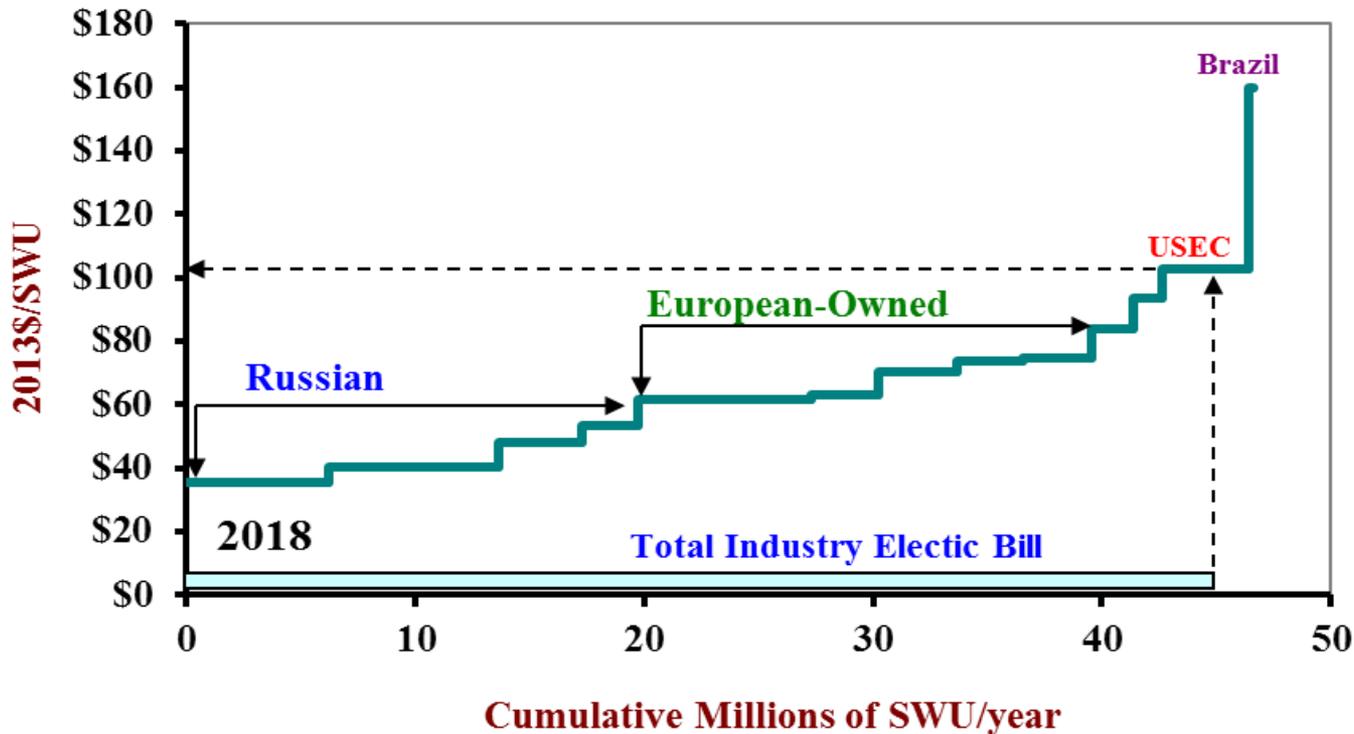
## Uranium Price Distribution, fitted with an exponential density:

Exponential[ \$69.60, Shift(\$25.50)], Mean = \$97, Median = \$73, SDev = \$74



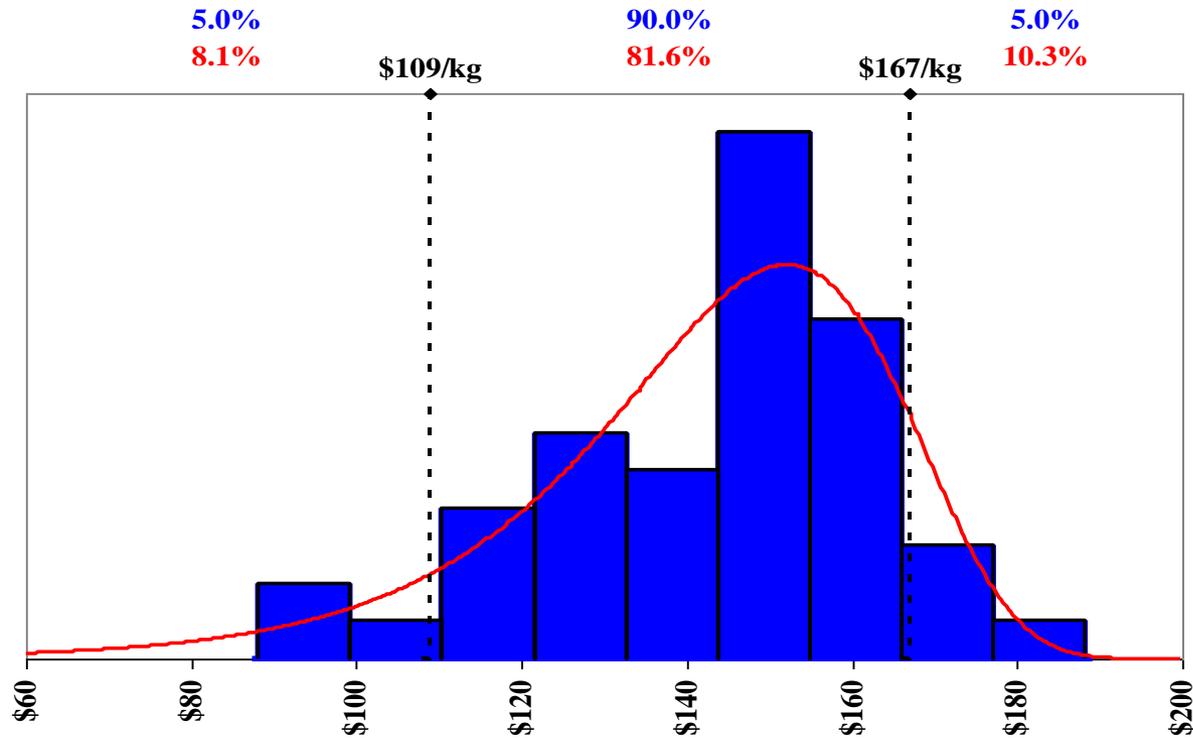
## The Uranium Enrichment Market, measured in Separative Work Units, SWU:

Rothwell, G.S. 2009. "Market Power in Uranium Enrichment," *Science & Global Security* 17(2-3): 132-154. <http://scienceandglobalsecurity.org/ru/archive/sgrs17rothwell.pdf>



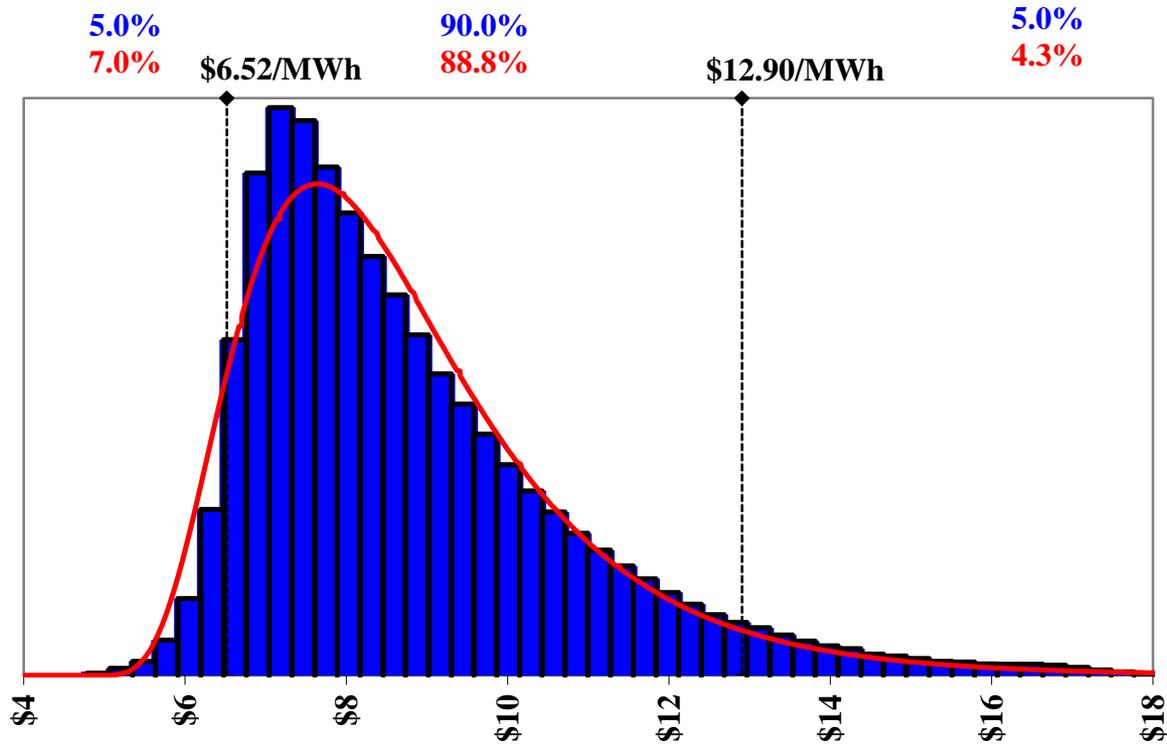
## Separative Work Unit Price Distribution, fitted with a minimum extreme value density:

Extreme Value,  $\text{minv}(\$152.40, \$17.59)$ , Mean = \$143, SDev = \$20



## Calculated Nuclear Fuel Price Distribution, fitted to a lognormal density:

Lognormal(\$4.23, \$2.02, Shift(\$4.57)), Mean = \$8.80, Mode = \$7.27, SDev = \$2.04



## ALWR O&M Costs:

$$\begin{aligned}
 O\&M &= (p_L \cdot L) + M \\
 O\&M &= (1 + om) (p_L \cdot L)
 \end{aligned}$$

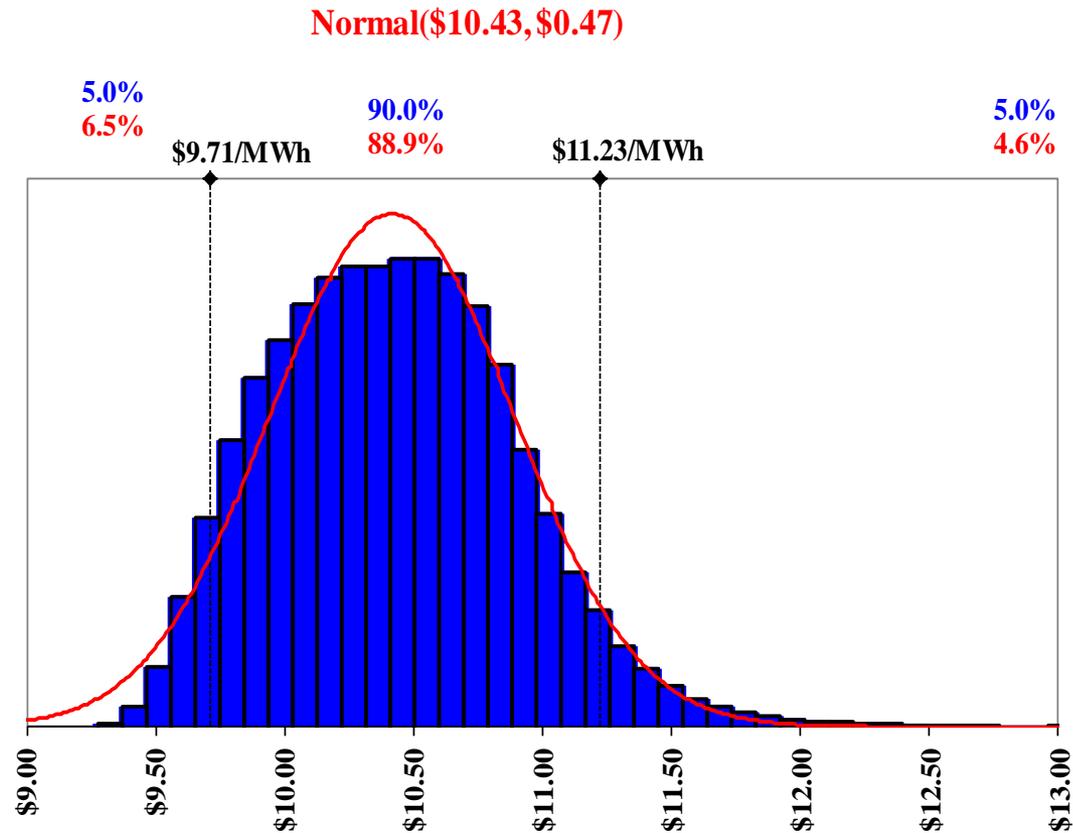
- (1)  $p_L$  is the average employee wages and benefits
- (2)  $L$  is the number of plant employees
- (3)  $M$  includes maintenance materials, capital additions, supplies, operating fees, property taxes, and insurance
- (4)  $om$  is 0.65 (varies in simulation uniformly between 0.55 and 0.75)

$$\begin{aligned}
 \ln(L) &= 5.547 + 0.870 (GW) & R^2 &= 96\% \\
 &(0.181) \quad (0.099) & \text{Standard Error} &= 12.43\%
 \end{aligned}$$

- (1)  $\ln(L)$  is the natural logarithm of the number of employees and
- (2)  $GW$  is the size of the plant in gigawatt

$$\begin{aligned}
 p_L \cdot L &= p_L \cdot e^{5.55} \cdot e^{(0.87)(1.2)} = \$80,000 \cdot 730 = \$58.4 \text{ M} \\
 O\&M &= (1 + om) (p_L \cdot L) = 1.65 \cdot \$58.4 \text{ M} = \$96.4 \text{ M}
 \end{aligned}$$

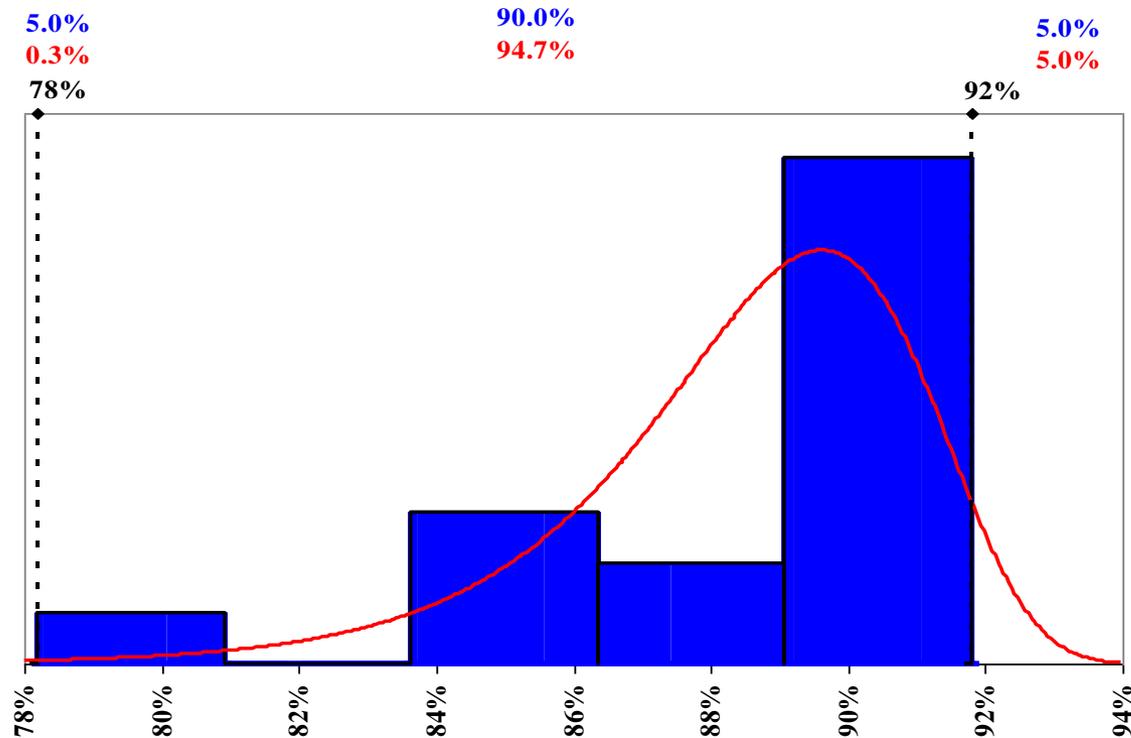
## Calculated Operation and Maintenance Cost Distribution, fitted with a normal density:



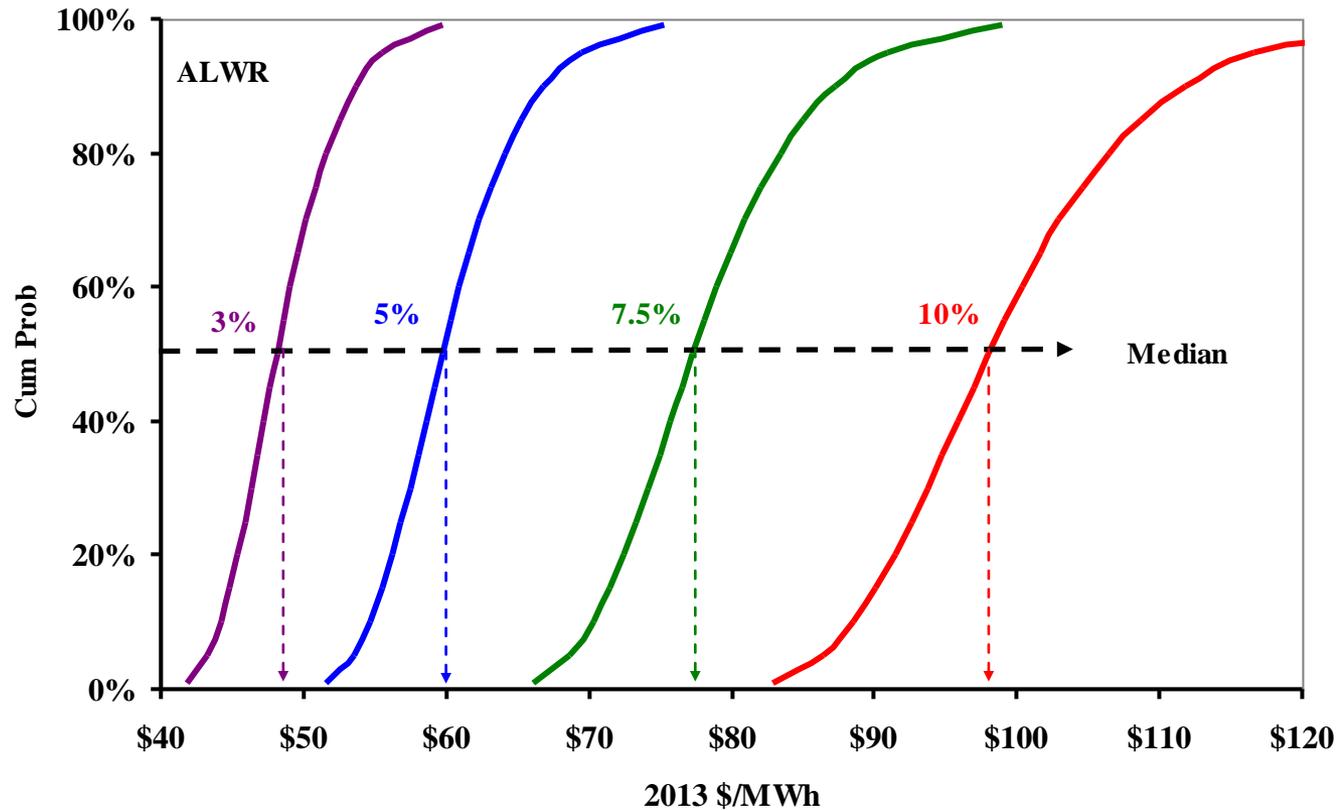
## Nuclear Power Plant Capacity Factor Distribution, fitted with a minimum extreme value density:

Source: <http://www.eia.gov/totalenergy/data/monthly/pdf/sec8.pdf>

Extreme Value, minv(89.6%, 2.5%), Mean = 89%, SDev = 3.3%, Min = 78%, Max = 92%

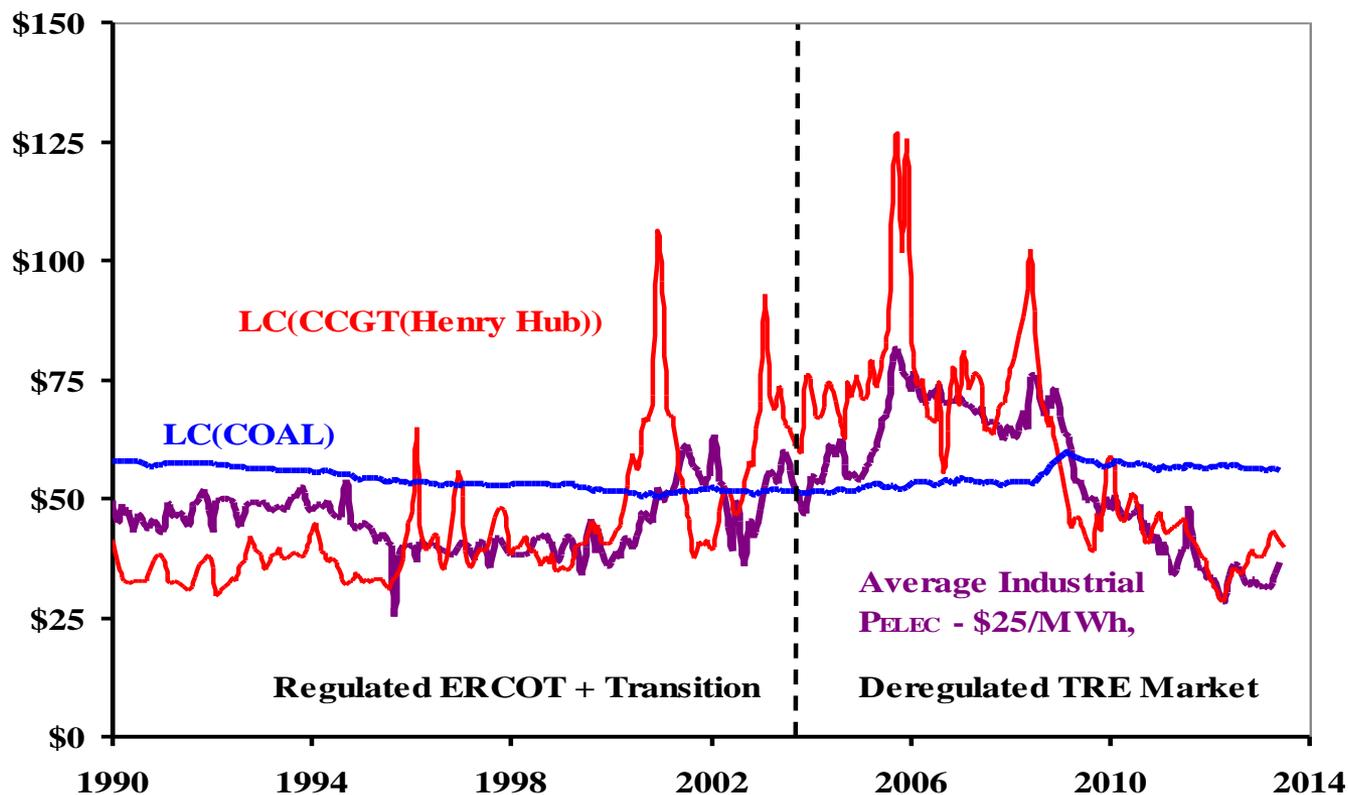


## Cumulative Distributions for Levelized Costs of ALWRs:



## Electricity Prices and Levelized Costs

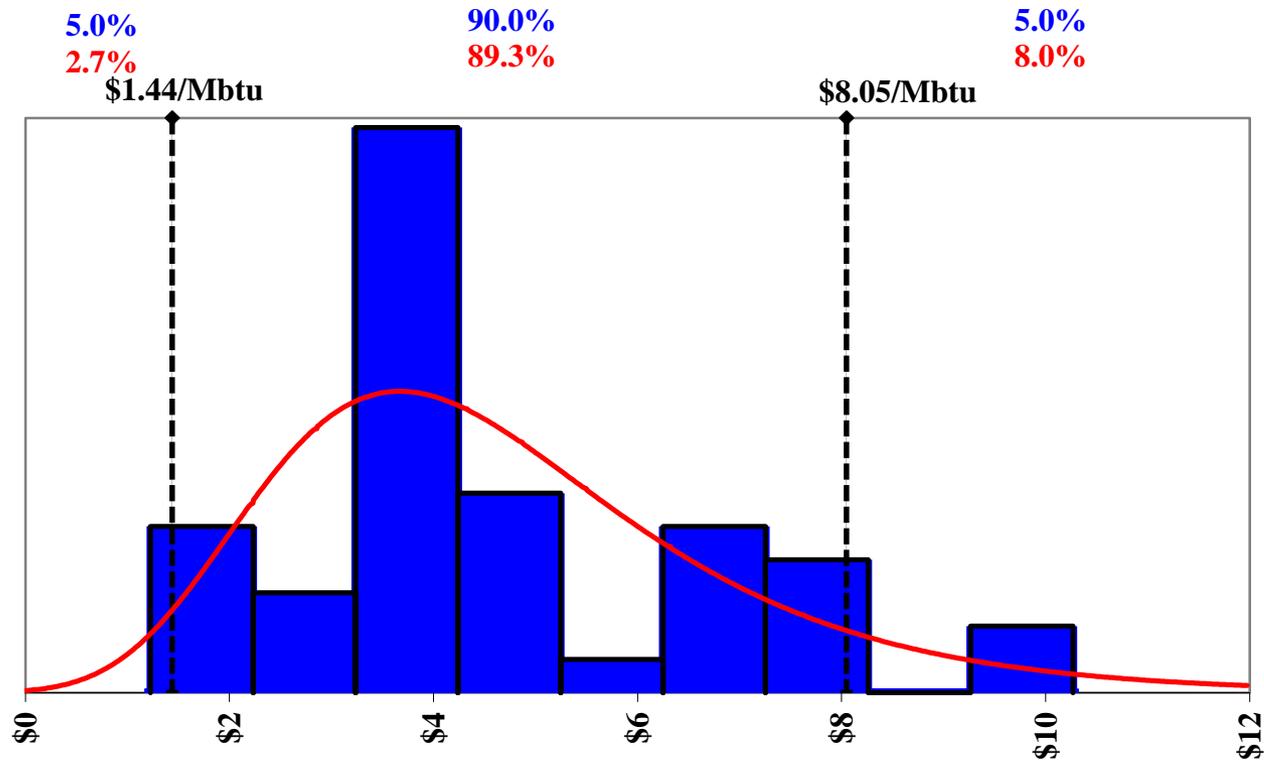
e.g., Electricity Prices in Texas ERCOT/TRE, 1990-2013,  
**mean was \$74.18/MWh with a standard deviation of \$11.83/MWh**  
*Source: <http://www.eia.gov/electricity/data.cfm#sales>*



## Natural Gas Prices, fitted with an extreme value density:

Source: <http://www.eia.gov/state/seds/seds-data-fuel.cfm?sid=US>

Extreme Value, maxv(\$3.69, \$1.75), Mean = \$4.71, SDev = \$2.25, Mode = \$6.41



## Texas Coal Prices, fitted with an extreme value density:

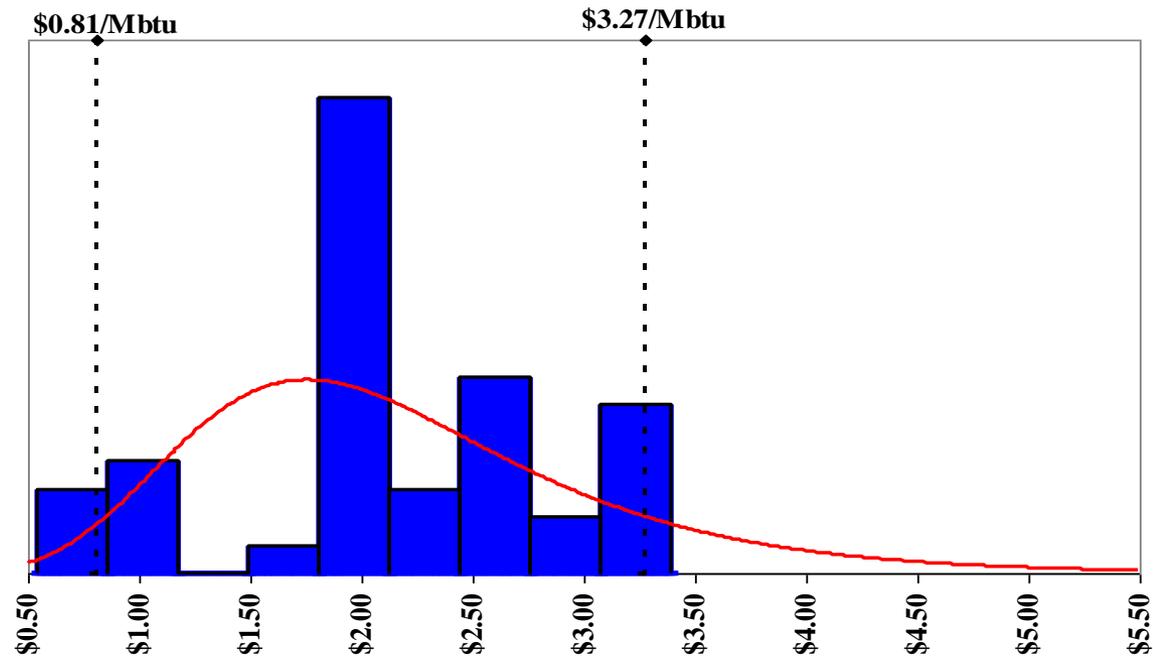
Source: <http://www.eia.gov/state/seds/seds-data-fuel.cfm?sid=US>

Extreme Value( \$1.76 \$0.72), Mean = \$2.15, Mode = \$1.90, SDev = \$0.72

5.0%  
2.3%

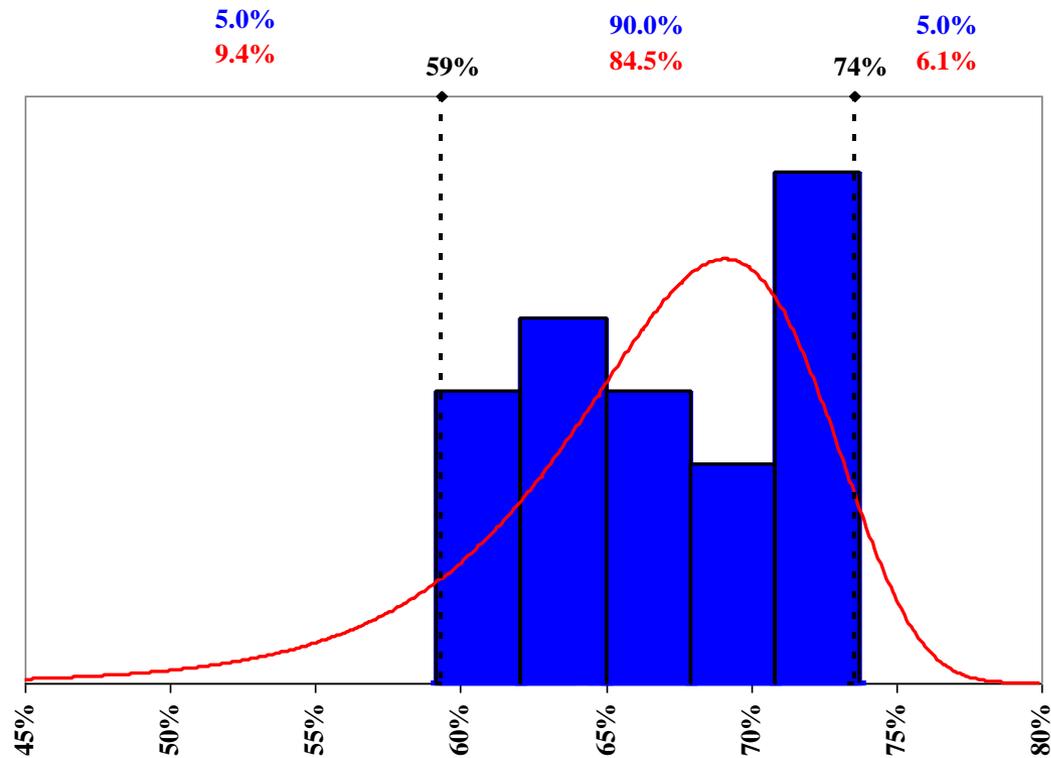
90.0%  
86.0%

5.0%  
11.7%



## CCGT and Coal Plant Capacity Factors, fitted with a minimum extreme value density: *Source: <http://www.eia.gov/totalenergy/reports.cfm?t=182>*

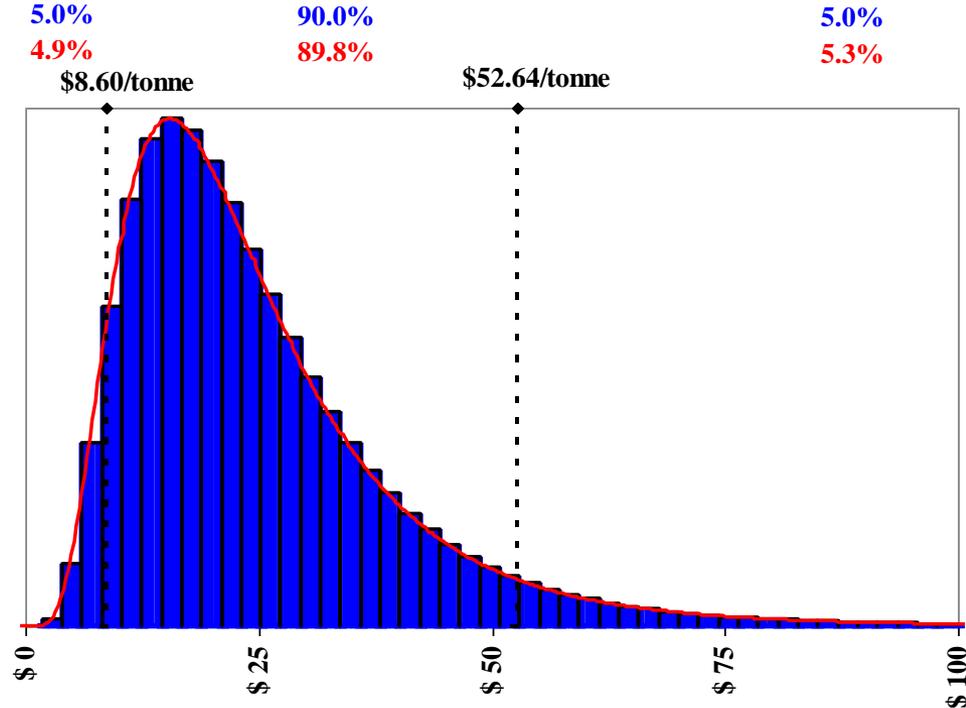
Extreme Value, minv( 69%, 4%), Mean = 66.8%, SDev = 5%, Min = 59.2%, Max = 73.7%



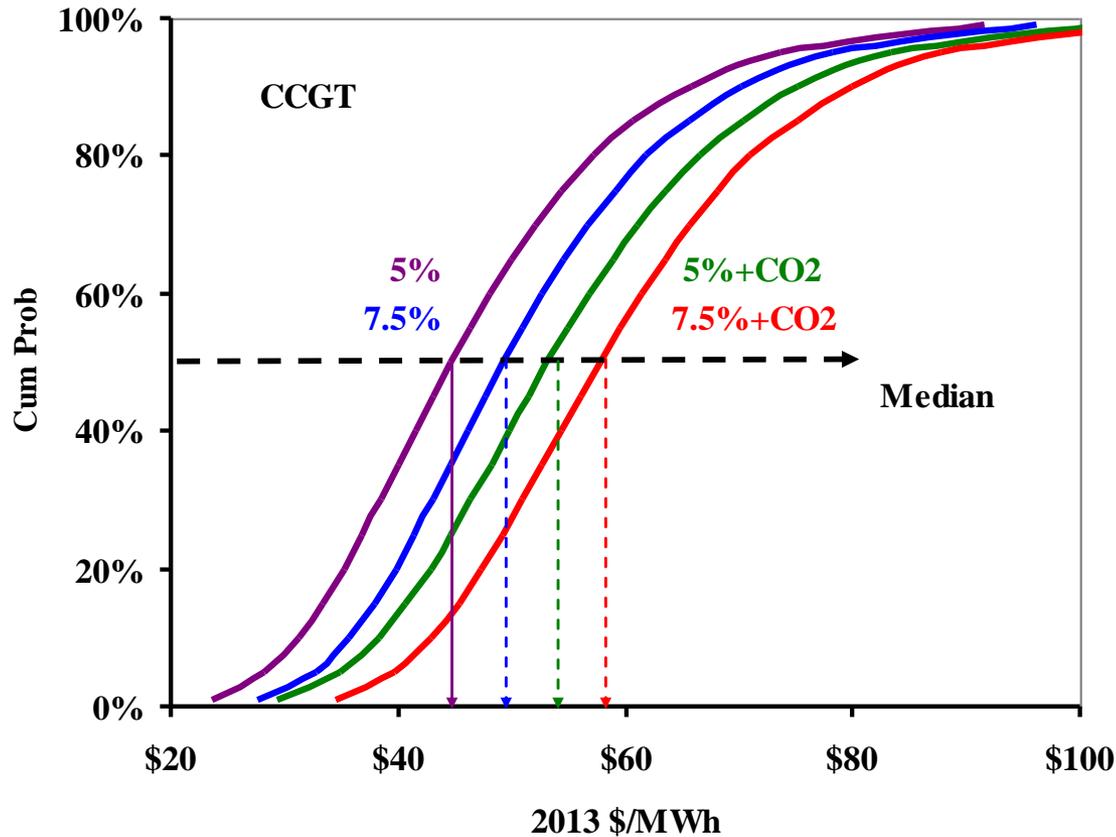
## Proposed Carbon Dioxide Cost Distribution, modelled with a Log-Normal density:

**Sources: \$25 mean from MIT(2009) with SDev = \$15, Nordhaus (2011) Figure 5**

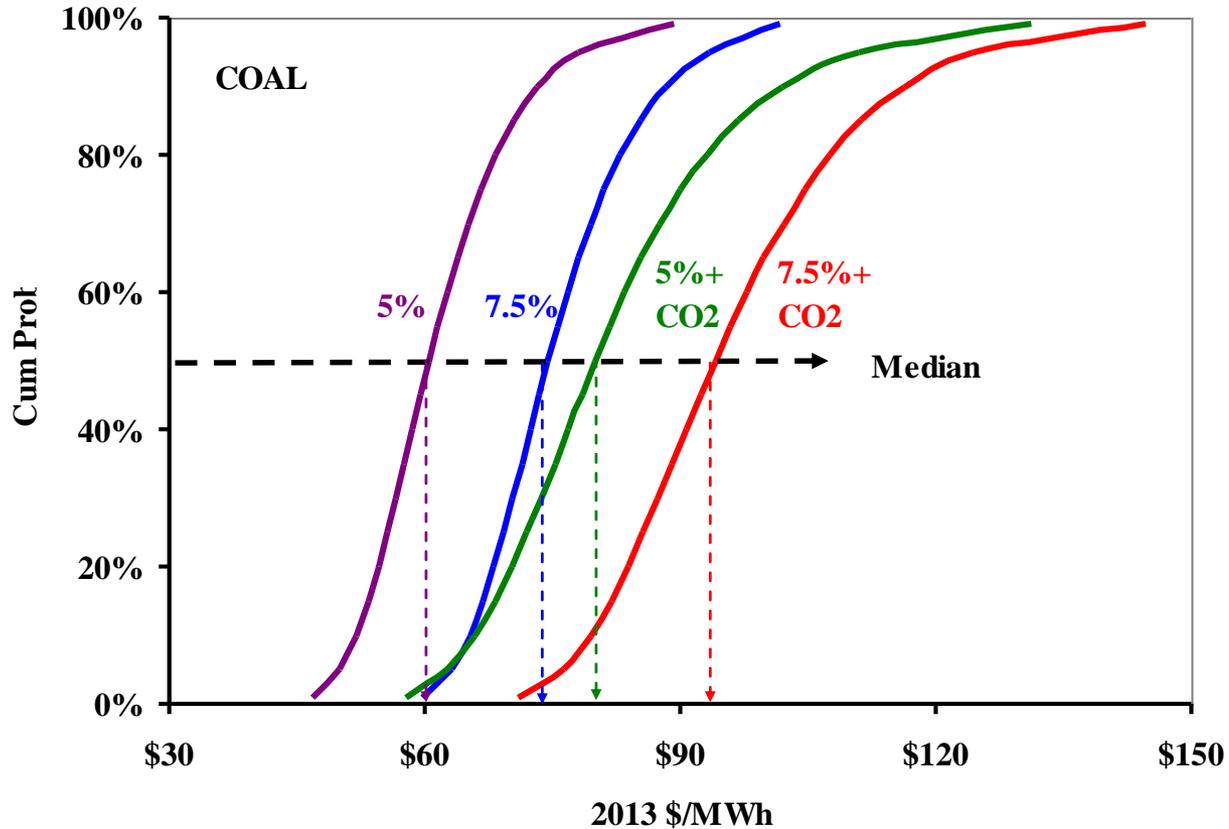
Lognormal( \$25, \$15), Mode = \$16, Median = \$21, Mean = \$25, Min = \$2, Max = \$100



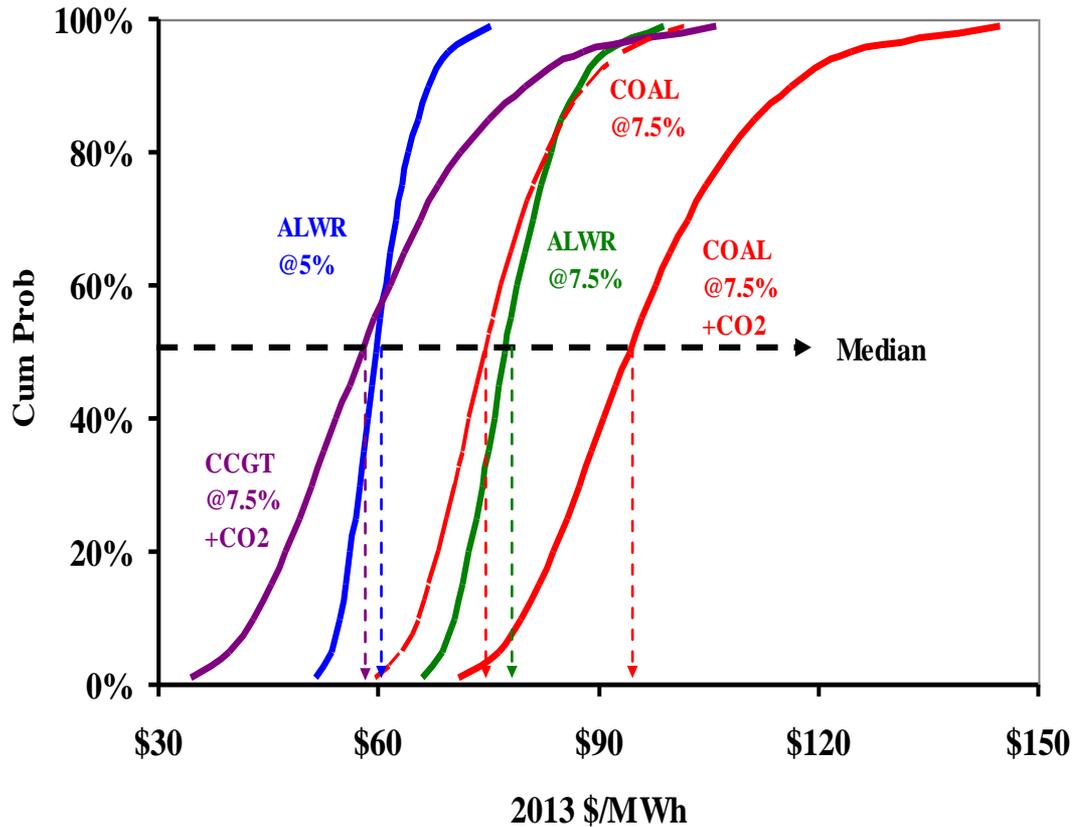
## Cumulative Distributions for Levelized Costs of Combined Cycle (Natural) Gas Turbine:



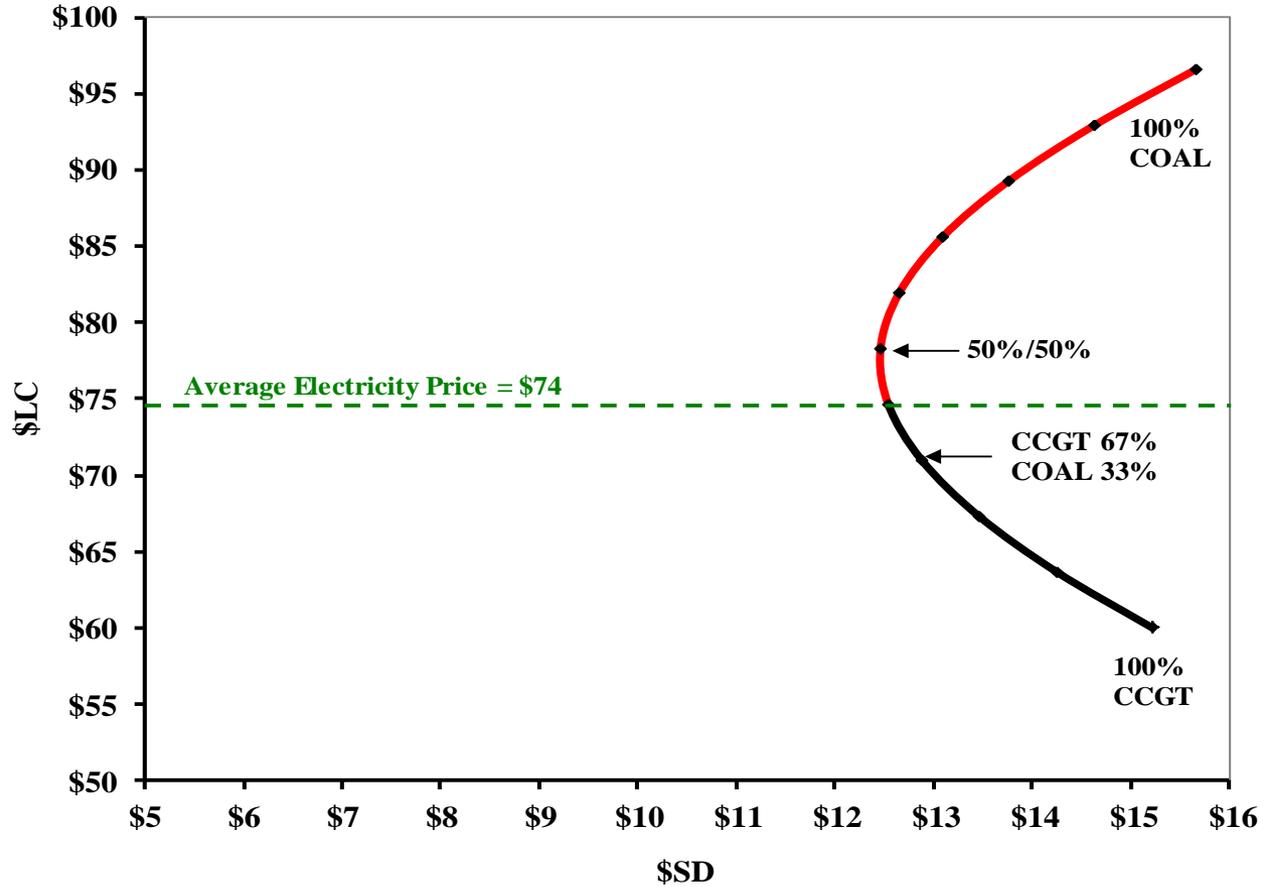
## Cumulative Distributions for Levelized Costs of Coal with Advanced Pollution Controls:



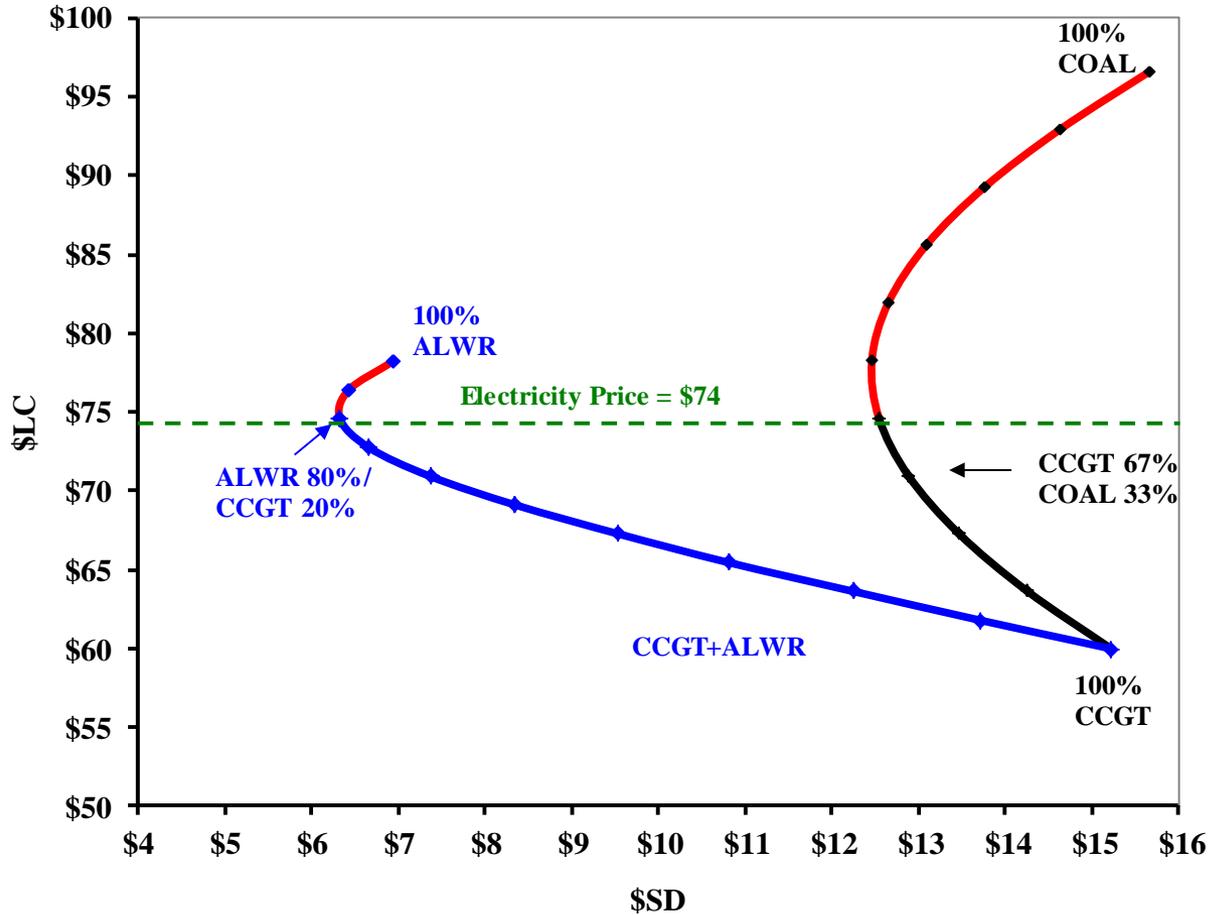
## ALWR, CCGT, and Coal Levelized Costs: simulated cumulative distributions with and without CO<sub>2</sub> Fee



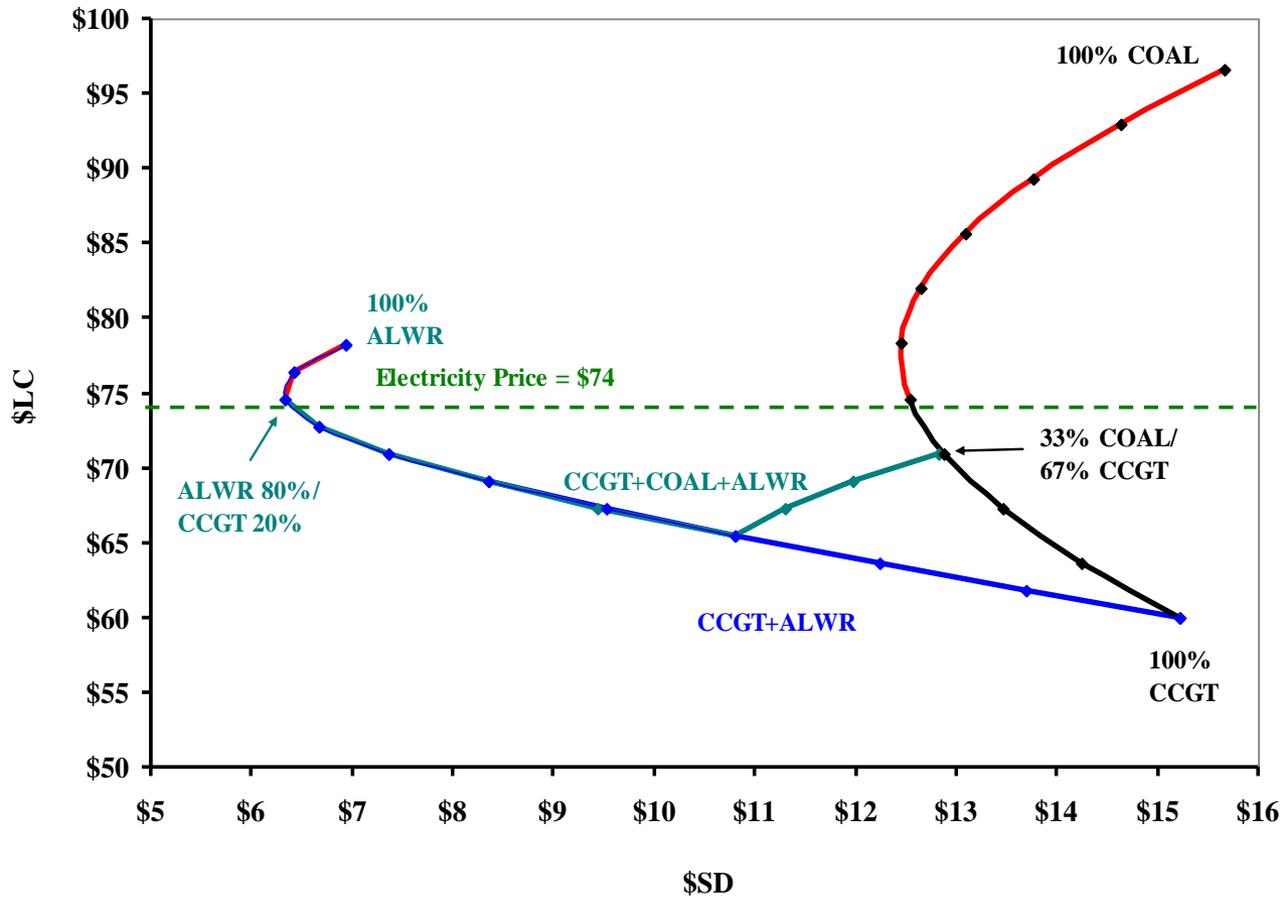
## Levelized Cost and Risk with Portfolios of CCGT and Coal:



## Levelized Cost and Risk with Portfolios of CCGT, Coal, and ALWRs (7.5%):



## Levelized Cost and Risk with Portfolios of CCGT, Coal, and ALWRs (7.5%):



## U.S. Nuclear Power Costs: Blurred Bottom Lines

- **Natural gas prices are volatile and will rise** (1) as U.S. petro-chemical industries shift from oil to gas and (2) as the U.S. exports Liquefied Natural Gas to Asia and Europe.
- With increases in gashouse gas costs (and prices) portfolios of electricity generating assets with **nuclear power costs will lower the volatility of electricity costs** making industry more competitive, energy supply more secure, and until electricity storage is developed, electricity systems more sustainable.

## **Further Research:**

- **Specify Correlations, e.g., between Construction Costs and Lead Time**
- **Add wind to portfolio analysis**
- **Add load duration & system effects**
- **Add competitive electricity markets**
- **Endogenize the Cost of Capital**
- **Others? Suggestions?**

**Thank you for your attention, for more, see**

**Rothwell and Ganda, “Electricity Generating Portfolios with Small Modular Reactors” (June 2014), available at <http://energy.gov/ne/downloads/electricity-generating-portfolios-small-modular-reactors>**

**This paper provides a method for estimating the probability distributions of the levelized costs of electricity. These probability distributions can be used to find cost-risk minimizing portfolios of electricity generating assets including Combined-Cycle Gas Turbines (burning natural gas), coal-fired power plants with sulphur scrubbers, and Small Modular Reactors, SMRs. Probability densities are proposed for a dozen electricity generation cost drivers, including fuel prices and externalities costs. Given the long time horizons involved in the planning, construction, operation, refurbishment, and post-retirement management of generating assets, price data from the last half century are used to represent long-run price probabilities. This paper shows that SMRs can competitively replace coal units in a portfolio of coal and natural gas generating stations to reduce the levelized cost risk associated with the volatility of natural gas prices and unknown carbon costs.**